

# PARTIAL CO-REPRESENTATIONS OF HOPF ALGEBRAS

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Abstract: Partial actions arose in operator algebra study by Exel in [3] and it was extended to a purely algebraic context by Dockuchaev and Exel in [4]. The study of such a new structure has been developed in several directions, as the partial representation of partial group actions by Dockuchaev, Exel and Piccione in [5]. In [2], Caenepeel and Janseen developed the notion of partial actions of Hopf algebras on algebras, unifying partial actions of groups and actions of Hopf algebras. This new concept generates a rich theory, triggering the study of several aspects of this new structure.

In [1], Alves, Batista and Verduynse developed the concept of partial representation of Hopf algebras, retrieving properties from partial representation of groups to this new setting. In that work, the authors defined a partial representation of a Hopf algebra  $H$  on an algebra  $A$  as a linear transformation  $\pi: H \rightarrow A$  satisfying appropriated conditions. The authors defined the notion of partial  $H$ -module via partial representations of  $H$  on the endomorphism algebra  $\text{End}(A)$ , they constructed the category of partial  $H$ -modules, they constructed a universal algebra ( $H_{\text{par}}$ ) on which every partial representation is factorized and they showed  $H_{\text{par}}$  has a structure of Hopf algebroid.

The aim of this work is to present the study in development about the partial co-representations of coalgebras on Hopf algebras, exposing the properties and examples developed. A partial co-representation of a coalgebra  $C$  on a Hopf algebra  $H$  is defined as a linear transformation  $\omega: C \rightarrow H$  satisfying several conditions, duals of those presented in [1]. The initial examples are got from well-known partial structures, so examples of partial co-representation are obtained from partial representations and from partial coactions on coalgebras. In this work, we develop the notion of partial  $H$ -comodules, we construct a universal coalgebra  $H^{\text{par}}$  that factorizes every partial co-representation by coalgebra morphisms, we show that the category of partial comodules is isomorphic to the category of  $H^{\text{par}}$ -comodules and show that it has a structure of Hopf coalgebroid.

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WORK IN COLLABORATION WITH MARCELO ALVES, ELIEZER BATISTA, GLAUBER QUADROS AND JOOST VERCRUYSSSE

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